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# Data Structures and Algorithms with Object-Oriented Design Patterns in Java

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*To my father,  
Indulis Preiss*



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# Preface

This book was motivated by my experience in teaching the course *EECE 250: Algorithms and Data Structures* in the Computer Engineering program at the University of Waterloo. I have observed that the advent of *object-oriented methods* and the emergence of object-oriented *design patterns* has led to a profound change in the pedagogy of data structures and algorithms. The successful application of these techniques gives rise to a kind of cognitive unification: Ideas that are disparate and apparently unrelated seem to come together when the appropriate design patterns and abstractions are used.

This paradigm shift is both evolutionary and revolutionary. On the one hand, the knowledge base grows incrementally as programmers and researchers invent new algorithms and data structures. On the other hand, the proper use of object-oriented techniques requires a fundamental change in the way the programs are designed and implemented. Programmers who are well schooled in the procedural ways often find the leap to objects to be a difficult one.

## ❖ Goals

The primary goal of this book is to promote object-oriented design using Java and to illustrate the use of the emerging *object-oriented design patterns*. Experienced object-oriented programmers find that certain ways of doing things work best and that these ways occur over and over again. The book shows how these patterns are used to create good software designs. In particular, the following design patterns are used throughout the text: *singleton*, *container*, *enumeration*, *adapter* and *visitor*.

Virtually all of the data structures are presented in the context of a *single, unified, polymorphic class hierarchy*. This framework clearly shows the *relationships* between data structures and it illustrates how polymorphism and inheritance can be used effectively. In addition, *algorithmic abstraction* is used extensively when presenting classes of algorithms. By using algorithmic abstraction, it is possible to describe a generic algorithm without having to worry about the details of a particular concrete realization of that algorithm.

A secondary goal of the book is to present mathematical tools *just in time*. Analysis techniques and proofs are presented as needed and in the proper context. In the past when the topics in this book were taught at the graduate level, an author could rely on students having the needed background in mathematics. However, because the book is targeted for second- and third-year students, it is necessary to fill in the background as needed. To the extent possible without compromising correctness, the presentation fosters intuitive understanding of the concepts rather than mathematical rigor.

## ❖ Approach

One cannot learn to program just by reading a book. It is a skill that must be developed by practice. Nevertheless, the best practitioners study the works of others and incorporate their observations into their own practice. I firmly believe that after learning the rudiments of program writing, students should be exposed to examples of complex, yet well-designed program artifacts so that they can learn about the designing good software.

Consequently, this book presents the various data structures and algorithms as complete Java program fragments. All the program fragments presented in this book have been extracted automatically from the source code files of working and tested programs. It has been my experience that by developing the proper abstractions, it is possible to present the concepts as fully functional programs without resorting to *pseudo-code* or to hand-waving.

## ❖ Outline

This book presents material identified in the *Computing Curricula 1991* report of the ACM/IEEE-CS Joint Curriculum Task Force[43]. The book specifically addresses the following *knowledge units*: AL1: Basic Data structures, AL2: Abstract Data Types, AL3: Recursive Algorithms, AL4: Complexity Analysis, AL6: Sorting and Searching, and AL8: Problem-Solving Strategies. The breadth and depth of coverage is typical of what should appear in the second or third year of an undergraduate program in computer science/computer engineering.

In order to analyze a program, it is necessary to develop a model of the computer. Chapter 2 develops several models and illustrates with examples how these models predict performance. Both average-case and worst-case analyses of running time are considered. Recursive algorithms are discussed and it is shown how to solve a recurrence using repeated substitution. This chapter also reviews arithmetic and geometric series summations, Horner's rule and the properties of harmonic numbers.

Chapter 3 introduces asymptotic (big-oh) notation and shows by comparing with Chapter 2 that the results of asymptotic analysis are consistent with models of higher fidelity. In addition to  $O(\cdot)$ , this chapter also covers other asymptotic notations ( $\Omega(\cdot)$ ,  $\Theta(\cdot)$ , and  $o(\cdot)$ ) and develops the asymptotic properties of polynomials and logarithms.

Chapter 4 introduces the *foundational data structures*—the array and the linked list. Virtually all the data structures in the rest of the book can be implemented using either one of these foundational structures. This chapter also covers multi-dimensional arrays and matrices.

Chapter 5 deals with abstraction and data types. It presents the recurring design patterns used throughout the text as well a unifying framework for the data structures presented in the subsequent chapters. In particular, all of the data structures are viewed as *abstract containers*.

Chapter 6 discusses stacks, queues, and deques. This chapter presents implementations based on both foundational data structures (arrays and linked lists). Applications for stacks and queues are presented.

Chapter 7 covers ordered lists, both sorted and unsorted. In this chapter, a list is viewed as a *searchable container*. Again several applications of lists are presented.

Chapter 8 introduces hashing and the notion of a hash table. This chapter addresses the design of hashing functions for the various basic data types as well as

for the abstract data types described in Chapter 5. Both scatter tables and hash tables are covered in depth and analytical performance results are derived.

Chapter 9 introduces trees and describes their many forms. Both depth-first and breadth-first tree traversals are presented. Completely generic traversal algorithms based on the use of the *visitor* design pattern are presented, thereby illustrating the power of *algorithmic abstraction*. This chapter also shows how trees are used to represent mathematical expressions and illustrates the relationships between traversals and the various expression notations (prefix, infix, and postfix).

Chapter 10 addresses trees as *searchable containers*. Again, the power of *algorithmic abstraction* is demonstrated by showing the relationships between simple algorithms and balancing algorithms. This chapter also presents average case performance analyses and illustrates the solution of recurrences by telescoping.

Chapter 11 presents several priority queue implementations, including binary heaps, leftist heaps, and binomial queues. In particular this chapter illustrates how a more complicated data structure (leftist heap) extends an existing one (tree). Discrete-event simulation is presented as an application of priority queues.

Chapter 12 covers sets and multisets. Also covered are partitions and disjoint set algorithms. The latter topic illustrates again the use of algorithmic abstraction.

Garbage collection is discussed in Chapter 13. This is a topic that is not found often in texts of this sort. However, because the Java language relies on garbage collection, it is important to understand how it works and how it affects the running times of programs.

Chapter 14 surveys a number of algorithm design techniques. Included are brute-force and greedy algorithms, backtracking algorithms (including branch-and-bound), divide-and-conquer algorithms, and dynamic programming. An object-oriented approach based on the notion of an *abstract solution space* and an *abstract solver* unifies much of the discussion. This chapter also covers briefly random number generators, Monte Carlo methods, and simulated annealing.

Chapter 15 covers the major sorting algorithms in an object-oriented style based on the notion of an *abstract sorter*. Using the abstract sorter illustrates the relationships between the various classes of sorting algorithm and demonstrates the use of algorithmic abstractions.

Finally, Chapter 16 presents an overview of graphs and graph algorithms. Both depth-first and breadth-first graph traversals are presented. Topological sort is viewed as yet another special kind of traversal. Generic traversal algorithms based on the *visitor* design pattern are presented, once more illustrating *algorithmic abstraction*. This chapter also covers various shortest path algorithms and minimum-spanning-tree algorithms.

At the end of each chapter is a set of exercises and a set of programming projects. The exercises are designed to consolidate the concepts presented in the text. The programming projects generally require the student to extend the implementation given in the text.

## ❖ Suggested Course Outline

This text may be used in either a one semester or a two semester course. The course which I teach at Waterloo is a one-semester course that comprises 36 lecture hours on the following topics:

1. Review of the fundamentals of programming in Java and an overview of object-oriented programming with Java. (Appendix A). [4 lecture hours].
2. Models of the computer, algorithm analysis, and asymptotic notation (Chapters 2 and 3). [4 lecture hours].
3. Foundational data structures, abstraction, and abstract data types (Chapters 4 and 5). [4 lecture hours].
4. Stacks, queues, ordered lists, and sorted lists (Chapters 6 and 7). [3 lecture hours].
5. Hashing, hash tables, and scatter tables (Chapter 8). [3 lecture hours].
6. Trees and search trees (Chapters 9 and 10). [6 lecture hours].
7. Heaps and priority queues (Chapter 11). [3 lecture hours].
8. Algorithm design techniques (Chapter 14). [3 lecture hours].
9. Sorting algorithms and sorters (Chapter 15). [3 lecture hours].
10. Graphs and graph algorithms (Chapter 16). [3 lecture hours].

Depending on the background of students, a course instructor may find it necessary to review features of the Java language. For example, an understanding of *inner classes* is required for the implementation of *enumerations*. Similarly, students need to understand the workings of *classes*, *interfaces*, and *inheritance* in order to understand the unifying class hierarchy discussed in Chapter 5.

## ❖ Online Course Materials

Additional material supporting this book can be found on the world-wide web at the URL:

<http://www.pads.uwaterloo.ca/Bruno.Preiss/books/opus5>

In particular, you will find there the source code for all the program fragments in this book as well as an errata list.


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Thank you to all the students of E&CE 250 who were the guinea pigs on whom various parts of this book were tested. And finally, I apologize to my family and friends who suffered neglect while I single-mindedly pursued my goal.

A handwritten signature in black ink that reads "BRUNO". The letters are bold and stylized, with some overlapping and a casual, cursive feel.

Waterloo, Canada  
March 1, 1999